## Problem A. Abstract

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 2 seconds |
| Memory limit: | 256 mebibytes |

You have a DAG (Directed Acyclic Graph) with $n$ nodes and $m$ edges. The graph has exactly one node $x$ that has no outgoing edges. The $i$-th node has an integer value $a_{i}$ in it.
Every second, the following happens:

- For each node $i$, let $b_{i}=a_{i}$.
- For each node $i$, let $a_{i}=0$.
- For each node $i$, and each node $j$ such that there is an edge from $i$ to $j$, the value $b_{i}$ is added to $a_{j}$.
- The value $\left\lfloor\frac{b_{x}}{2}\right\rfloor$ is added to $a_{x}$.

Find the first moment of time when all $a_{i}$ become 0 . Since the answer can be very large, output it modulo 998244353.

## Input

The first line contains two integers $n$ and $m\left(1 \leq n \leq 10^{4} ; 1 \leq m \leq 10^{5}\right)$ : the number of vertices and edges in the graph.

The second line contains $n$ integers $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$ : the values in the vertices.
Each of the following $m$ lines contains two integers $u$ and $v(1 \leq u, v \leq n)$ which represent a directed edge from $u$ to $v$.
It is guaranteed that the graph is a DAG with no multi-edges, and there is exactly one node that has no outgoing edges.

## Output

Print a line with a single integer: the first moment of time when all $a_{i}$ become 0 , modulo 998244353 .

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## Examples

| standard input | standard output |
| :---: | :---: |
| 32 | 3 |
| 111 |  |
| 12 |  |
| 23 |  |
| 68 | 8 |
| 114514 |  |
| 14 |  |
| 15 |  |
| 23 |  |
| 25 |  |
| 34 |  |
| 45 |  |
| 46 |  |
| 56 |  |
| 56 | 9 |
| 72366 |  |
| 12 |  |
| 14 |  |
| 23 |  |
| 34 |  |
| 35 |  |
| 45 |  |

## Note

Hi, so to me seems like a notorious coincidence. (Codeforces 1704E)

## Problem B. Bocchi the Rock

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 10 seconds |
| Memory limit: | 512 mebibytes |

Given a circle divided into $n$ arcs by $n$ distinct points lying on it, your task is to determine the number of valid colorings that satisfy certain conditions. Each point on the circle can be colored either red or blue, and each arc can be colored either yellow or pink. Chords can be added between points of the same color, with the restriction that a chord cannot connect a red point and a blue point. No two chords can intersect. Additionally, each point should be connected to at most one chord. Once all chords are added, the circle is divided into various regions by these chords.
A coloring is considered good if it is possible to add chords in such a way that each region in the resulting division is monochrome. A region is considered monochrome if it does not include arcs of both colors. Your goal is to calculate the number of such good colorings, taking into account the designated colors of certain points and arcs.

Calculate the number of valid colorings modulo 998244353 , given the initial colors of some points and arcs.

## Input

The first line contains an integer $n\left(2 \leq n \leq 5 \cdot 10^{4}\right)$. The second line contains a string $s=s_{1} s_{2} \ldots s_{2 n}$, representing the color types of the arcs and points.
For every odd $i$, character $s_{i}$ can only be "Y", "P", or "?", meaning that the color of $\frac{i+1}{2}$-th arc is yellow, pink, or can be both colors, respectively.
For every even $i$, character $s_{i}$ can only be " R ", " B ", or "?", meaning that the color of $\frac{i}{2}$-th point is red, blue, or can be both colors, respectively.

## Output

Print a line with a single integer: the number of valid colorings modulo 998244353 .

## Examples

| standard input | standard output |
| :--- | :--- |
| 2 <br> $? ? ? ?$ | 12 |
| 3 <br> ??YR?B | 4 |
| 5 <br> YBYRPBYRYB | 0 |

## Note

In example 1, the 12 valid colorings are: YBYB, YBYR, YRYB, YRYR, PBPB, PBPR, PRPB, PRPR, YBPB, YRPR, PBYB, PRYR.

In example 2 , the following figures aid in visual understanding.


The left figure shows the circle before coloring; the middle figure represents a valid coloring as PBYRYB, and we can connect two points colored as B with a chord to prove that the coloring is good; the right figure represents an invalid coloring as PBYRPB.

## Problem C. Computer Network

Input file:
Output file:
standard input
Time limit:
Memory limit:
standard output
1 second
256 mebibytes
The additive-increase/multiplicative-decrease (AIMD) algorithm is a feedback control algorithm best known for its use in TCP congestion control. AIMD combines linear growth of the congestion window when there is no congestion with an exponential reduction when congestion is detected. Multiple flows using AIMD congestion control will eventually converge to an equal usage of a shared link. (from Wikipedia)
You are given two arrays of $n$ integers: $a$ and $b$. You can perform operations on the array $a$. In one operation, you can let $a_{i}$ become $a_{i}+1$ for all $1 \leq i \leq n$, or let $a_{i}$ become $\left\lfloor\frac{a_{i}}{2}\right\rfloor$ for all $1 \leq i \leq n$.
Find the minimum number of operations that you have to perform to transform $a$ into $b$, or determine that it is impossible.

## Input

The first line contains an integer $n\left(1 \leq n \leq 10^{6}\right)$.
The second line contains the integer array $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$.
The third line contains the integer array $b_{1}, b_{2}, \ldots, b_{n}\left(0 \leq b_{i} \leq 10^{9}\right)$.

## Output

Print the minimum number of operations needed, or -1 if it's impossible to transform $a$ into $b$.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{lllll} \hline 5 & & & \\ 1 & 2 & 3 & 4 & 5 \\ 6 & 6 & 6 & 6 & 7 \end{array}$ | 9 |
| $\begin{array}{lll} \hline 3 & & \\ 2 & 3 & 4 \\ 1 & 2 & 3 \end{array}$ | -1 |
| $\begin{array}{lll} \hline 2 & \\ 65536 & 65537 \\ 12 & \end{array}$ | 32 |

## Problem D. Digit DP

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
5 seconds
1024 mebibytes

There are $2^{n}$ machines in a factory, numbered from 0 to $2^{n}-1$. The $i$-th machine consumes $p_{i}$ units of power. The factory uses a system called Digit Dynamic Powering (Digit DP) to control the power the machines consume.
Initially, an array $a_{0}, \ldots, a_{n-1}$ is given. Then the system would set the initial $p_{i}$ to $\sum_{j \in S_{i}} a_{j}$, where $S_{i}$ is the set of 1 bits in the binary representation of $i$.
After that, there may be some modifications, each modification would be adding a certain value to the power of some machines that form an interval. Formally speaking, you would be given three integers $\ell$, $r, x$, meaning that the power consumed by each of the machines numbered between $\ell$ and $r$ (inclusively) should increase by $x$. The endpoints of the intervals would be given as $n$-digit binary strings.
When some three distinct machines are used to produce a product, the product's price should always be the product of the $p_{i}$ 's of those machines.

During these modifications, the manager may ask some questions about some intervals. What is the sum of the prices if we try every possible combination of three distinct machines in the interval to produce a product?
Formally speaking, you would be given two integers $\ell, r$, meaning that you should report the sum of the products $p_{i} \cdot p_{j} \cdot p_{k}$ of all triples $(i, j, k)$ satisfying $\ell \leq i<j<k \leq r$. As the answer may be rather large, find it modulo 998244353 . The endpoints of the intervals would also be given as $n$-digit binary strings.

## Input

The first line contains two integers $n$ and $q\left(1 \leq n \leq 100 ; 1 \leq q \leq 5 \cdot 10^{4}\right)$.
The second line contains the integer array $a_{0}, a_{1}, \ldots, a_{n-1}\left(0 \leq a_{i} \leq 10^{9}\right)$.
The next $q$ lines contain queries. On each line, the first integer $t$ indicates the type of the query.
If $t=1$, three integers $\ell, r, x$ follow $\left(0 \leq \ell \leq r<2^{n}, 0 \leq x \leq 10^{9}\right)$.
If $t=2$, two integers $\ell, r$ follow ( $0 \leq \ell \leq r<2^{n}$ ).
Note that $\ell$ and $r$ are given in $n$-bit binary string format, and the leftmost bit is the highest bit.

## Output

For each query of type 2, print a line with a single integer: the answer modulo 998244353.

## Examples

|  | standard input |  | standard output |  |
| :--- | :--- | :--- | :--- | :--- |
| 3 | 3 |  | 1960 |  |
| 1 | 2 | 4 |  | 3040 |
| 2 | 000 | 111 |  |  |
| 1 | 010 | 101 | 1 |  |
| 2 | 000 | 111 |  |  |
| 2 | 2 |  | 0 |  |
| 1 | 1 |  | 2 |  |
| 2 | 00 | 10 |  |  |
| 2 | 00 | 11 |  |  |

## Problem E. Except One

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 1 second |
| Memory limit: | 256 mebibytes |

You are given three integers $p, k, t$, where $p$ is a prime number.
The set $S$ is defined as follows: $S=\{x \mid x \in N, 1 \leq x \leq p-1, x \neq k\}$.
Find the sum of the products of all $t$-element subsets of $S$, modulo $p$.

## Input

The first line contains three integers $p, k, t$ ( $p$ is a prime number; $\left.1 \leq k \leq p-1 ; 1 \leq t \leq p-2 ; p \leq 10^{9}\right)$.

## Output

Print the sum of the products of all $t$-element subsets of $S$, modulo $p$.

## Examples

| standard input | standard output |
| :--- | :--- |
| 753 | 1 |
| 1167 | 3 |

## Problem F. Fun on Tree

Input file: standard input<br>Output file: standard output<br>Time limit: $\quad 7$ seconds<br>Memory limit: $\quad 256$ mebibytes

Beitou, renowned for its breathtaking beauty and abundant hot springs, attracts countless tourists seeking relaxation and rejuvenation. The region boasts an extraordinary concentration of hot springs and spas, making it a global hotspot for such indulgence. Once a quaint locale where locals sought solace in its natural hot springs, the Beitou Valley has blossomed into a sprawling expanse, now housing over thirty luxurious resorts.
Traditionally, hot springs evoke imagery of volcanic activity and the unmistakable scent of sulfur. However, for some, the latter proves rather unpleasant. You find yourself among those sensitive to the smell of sulfur, which brings us to your current predicament.

Presently visiting Beitou, you've obtained a map of this enchanting place, revealing a conceptual representation as a rooted tree. It's worth noting that Beitou's mystical aura allows for unconventional measurements, even enabling negative distances between nodes. Additionally, each node on the map comes with an associated sulfur content value.
An unexpected revelation leaves you questioning the accuracy of the sulfur content assigned to each location. In order to rectify this, your mission is to align the sulfur content with the newly acquired information. Moreover, you've uncovered intel about the location of the largest volcano in the vicinity. Prioritizing your safety and well-being, your ultimate goal is to pinpoint the spot farthest from this prominent volcano while having the lowest sulfur content. Your chosen evaluation metric for each node's viability is given by the formula $d_{i}-a_{i}$, wherein $d_{i}$ represents the distance between node $i$ and the largest volcano, and $a_{i}$ is the corresponding sulfur content value.

We can describe each piece of new information you acquire with three integers, $x_{i}, y_{i}$, and $v_{i}$. It means that all the subtree of $y_{i}$ now has $v_{i}$ more sulfur (if $v_{i}$ is negative, then the sulfur content value decreases). Besides, you also learn that the largest volcano is actually located at $x_{i}$.
Note that the modifications of sulfur value are persistent: when you get another piece of new information, the sulfur modifications from the previous ones still apply.

## Input

The first line contains two integers $n$ and $q\left(2 \leq n \leq 2 \cdot 10^{5}\right.$ and $\left.0 \leq q \leq 2 \cdot 10^{5}\right)$ : the size of the tree and the number of queries.
The second line contains $n$ integers $a_{1}, a_{2}, \ldots, a_{n}\left(\left|a_{i}\right| \leq 10^{9}\right)$ : the sulfur content value of each nodes.
Next, $n-1$ lines are given. The $i$-th of these lines contains two integers $p_{i+1}$ and $w_{i+1}\left(1 \leq p_{i+1} \leq i\right.$ and $\left.\left|w_{i+1}\right| \leq 10^{9}\right)$ : the parent node of vertex $i+1$ and the distance between $p_{i+1}$ and $i+1$.

Finally, $q$ lines are given. Each line contains three integers $x_{i}, y_{i}$, and $v_{i}\left(1 \leq x_{i}, y_{i} \leq n\right.$ and $\left.\left|v_{i}\right| \leq 10^{9}\right)$ : the new piece of information you acquired.

## Output

For each new piece of information, print a line with two integers $s_{i}$ and $d_{i}$ : the index of the node having the largest viability and the viability itself.
If there are multiple answers, please output the one with the minimal node index.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{\|llllll} \hline 6 & 6 & & & & \\ 1 & 1 & 4 & 5 & 1 & 4 \\ 1 & 5 & & & & \\ 2 & 0 & & & & \\ 3 & 2 & & & & \\ 4 & 1 & & & & \\ 5 & 6 & & & \\ 3 & 2 & -100000 \\ 1 & 2 & 100000 \\ 1 & 1 & 0 & & \\ 2 & 2 & 66 & & \\ 3 & 1 & 5 & & \\ 4 & 4 & -3 & & \end{array}$ | $\begin{array}{ll} 6 & 100005 \\ 6 & 10 \\ 6 & 10 \\ 1 & 4 \\ 1 & -1 \\ 1 & 1 \end{array}$ |
| $\begin{array}{llllll} \hline 5 & 6 & & & \\ -10 & 0 & 2 & -4 & 8 \\ 1 & 7 & & & \\ 1 & 1 & & & \\ 2 & 2 & & & \\ 2 & -2 & & & \\ 1 & 1 & 100 & \\ 2 & 1 & -100 \\ 1 & 1 & 0 & & \\ 4 & 3 & 10 & & \\ 2 & 5 & 3 & & \\ 5 & 2 & 2 & & \end{array}$ | $\begin{array}{ll} \hline 4 & -87 \\ 1 & 17 \\ 4 & 13 \\ 1 & 19 \\ 1 & 17 \\ 1 & 15 \end{array}$ |
| $\begin{array}{llllll} \hline 6 & 3 & & & \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 10 & & & \\ 1 & 10 & & & \\ 1 & -100 & & \\ 4 & 10 & & & \\ 4 & 11 & & & \\ 1 & 1 & 0 & & \\ 4 & 1 & 0 & & \\ 1 & 4 & 1000 & & \end{array}$ | $\begin{array}{\|ll\|} \hline 2 & 10 \\ 6 & 11 \\ 2 & 10 \\ \hline \end{array}$ |

## Problem G. Game

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 25 seconds |
| Memory limit: | 512 mebibytes |

A new game called Boundle works as follows. In each turn, the player tells the host a string of length 5 consisting of uppercase English alphabets. Then, the host should respond with a string of length 5 consisting of $<,=,>$, indicating the alphabetical order compared to the answer string in the host's mind in each position. The answer string should be the same throughout the game, and should also consist of uppercase English alphabets.

Two sisters, Yui and Ui are going to play a game of Boundle. The elder sister Yui will be the host, and the younger sister Ui will be the player. Ui has a set of $n$ strings she would use as queries, and for each of the $n$ strings in Ui's set, Yui has already set a fixed response. Here's the twist though: as Yui is careless, it is guaranteed that there actually does not exist a string that matches all of her fixed responses.
Every turn, Ui randomly and uniformly chooses a string in her set that has not yet been chosen, and receives the fixed response for that string. For each $i$ from 1 to $n$, calculate the number of ways the game is played if Ui realizes just after the $i$-th turn that the responses given by her elder sister Yui are not consistent. Ui is smart enough, so, when the responses don't add up, she immediately sees that Yui does not actually have an answer string in her mind.

Note that it is guaranteed that if Ui finishes all the strings in the set, the results she gets will not be consistent.
Also, for some mysterious reasons, unlike the original game, even if the responses have already narrowed the possible answer strings down to one possibility, the game would still continue until all the strings in the set have been chosen, or the responses become inconsistent.

## Input

The first line contains an integer $n\left(1 \leq n \leq 10^{5}\right)$.
Subsequently, there are $n$ lines, with each line containing two strings. The first string belongs to the set of strings from Ui, and the second string represents Yui's response to it.
All strings in Ui's set are distinct and consist of five uppercase English alphabets. Yui's responses are strings of length 5 , containing only the characters " $<$ ", " $=$ ", and " $>$ ".

It is guaranteed that there does not exist a string that matches all of Yui's responses.

## Output

Print a line with $n$ integers, the $i$-th of which should be the number of ways the game can be played if Ui realizes Yui is lying just after the $i$-th turn.
Print all numbers modulo 998244353.

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Cup

## Examples



## Problem H. Harumachi Kaze

Input file: standard input<br>Output file: standard output<br>Time limit: 30 seconds<br>Memory limit: $\quad 256$ mebibytes

This is an interactive problem.
You are given two arrays $a$ and $b$ of length $n$, consisting of non-negative integers.
There is a hidden permutation of integers from 0 to $2^{64}-1$ : $p(0), p(1), \ldots, p\left(2^{64}-1\right)$. You only know that $p(0)=0$.

Since $p$ is a permutation, $p^{-1}$ can also be defined: $p^{-1}(x)=y$ when $p(y)=x$.
Also, you are given an integer $B$. A positive integer $x$ is called cute if and only if the two following conditions hold:

- The binary representation of $x$, when viewed as a string of length $B$, is a palindrome.
- If a bit in the binary representation of $x$ is 1 , this bit must either be in the first 6 bits or in the last 6 bits. For example, if $B=14$, the two bits in the center must both be 0 .

You have to support queries of two types.
The first type of query is to change an element in one of the arrays.
The second type of query is to answer the following question: if we list $2 n$ integers, $p\left(a_{1}\right), p\left(a_{1}\right)+p\left(a_{2}\right), \ldots$, $p\left(a_{1}\right)+p\left(a_{2}\right)+\ldots+p\left(a_{n}\right)$ and $p\left(b_{1}\right), p\left(b_{1}\right)+p\left(b_{2}\right), \ldots, p\left(b_{1}\right)+p\left(b_{2}\right)+\ldots+p\left(b_{n}\right)$, and sort them into $c_{1}, c_{2}, \ldots, c_{2 n}$, what would $p^{-1}\left(c_{k}\right)$ be? It is guaranteed that $k$ is a cute number.
There are two interaction functions for you to call.

- $\operatorname{add}(x, y):$ returns $p^{-1}(p(x)+p(y))$.
- $\operatorname{cmp}(x, y):$ returns $p^{-1}(\min (p(x), p(y)))$.

Please beware that it is invalid to ask $\operatorname{add}(x, y)$ if $p(x)+p(y) \geq 2^{64}$.
To help you refrain from making invalid calls, it is guaranteed that, at any moment, the following condition holds: $\max \left(p\left(a_{1}\right)+p\left(a_{2}\right)+\ldots+p\left(a_{n}\right), p\left(b_{1}\right)+p\left(b_{2}\right)+\ldots+p\left(b_{n}\right)\right)<2^{64}$.

## Input

You begin the interaction by reading three integers: $n, q, B\left(1 \leq n \leq 1 \cdot 6 \cdot 10^{4} ; 1 \leq q \leq 2 \cdot 10^{4} ; 1 \leq B \leq 16\right)$. Then, you should read two lines, the first containing the array $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i}<2^{64}\right)$, and the second containing the array $b_{1}, b_{2}, \ldots, b_{n}\left(0 \leq b_{i}<2^{64}\right)$.

After that, you should read the contents of the $q$ queries.
For the next $q$ lines, the first integer type indicates the type of query $(1 \leq$ type $\leq 2)$.

- If type $=1$, three integers follow: $t$, pos, $x\left(1 \leq t \leq 2 ; 1 \leq\right.$ pos $\left.\leq n ; 0 \leq x<2^{64}\right)$.
- If $t=1$, set $a_{p o s}=x$.
- If $t=2$, set $b_{\text {pos }}=x$.
- If type $=2$, one integer $k$ follows $\left(1 \leq k \leq \min \left(2^{B}-1,2 \cdot n\right)\right)$. It is guaranteed that $k$ is a cute number.

It is guaranteed that there is at least 1 and at most 5000 queries of type 1.

## Interaction Protocol

After reading all the input, you can make at most $1.6 \cdot 10^{6}$ function calls.
For each call, you print a line of the form " $t x y$ ", where $t$ is either "A" or "C", and $x$ and $y$ are integers $\left(0 \leq x, y<2^{64}\right)$. Then flush the output, and read a line with the resulting integer $z$ :

- If $t$ is " A ", you will get $z=p^{-1}(p(x)+p(y))$.
- If $t$ is " C ", you will get $z=p^{-1}(\min (p(x), p(y)))$.

If you make too many calls or make an invalid call, you will receive the Wrong Answer verdict.
After you have calculated the answers to all queries of type 2, print two lines. The first line should be "! $m$ ", where $m$ is the number of type 2 queries. The second line should contain $m$ integers $q_{1}, \ldots, q_{m}$ : the answers to the type 2 queries respectively. Note that printing the answer does not count towards your total of $1.6 \cdot 10^{6}$ calls. After printing these two lines, your program should terminate.

## Example

$\left.\begin{array}{|lll|lll|}\hline & \text { standard input } & & \text { standard output } \\ \hline 2 & 3 & 2 & & & \\ 1 & 3 & & & \\ 5 & 7 & & & \\ 2 & 3 & 2 & 9 & \text { A } 1 & 3\end{array}\right]$

## Problem I. Interval Addition

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 4 seconds |
| Memory limit: | 512 mebibytes |

You are given an array $a$ of $n$ integers. You can perform operations on this array. In a single operation, you can add any real number $x$ to some consecutive interval of $a$.
Determine the minimum number of operations that have to be performed to make all elements of $a$ equal to 0 .

## Input

The first line contains an integer $n(1 \leq n \leq 23)$.
The second line contains the array $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$.

## Output

Print a line with a single integer: the minimum number of operations needed.

## Examples

|  |  |  |  |  |  |  | standard input |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  | 3 | standard output |
|  | 2 | 3 | 2 | 1 |  | 4 |  |
| 6 |  |  |  |  |  |  |  |
| 1 | 1 | 4 | 5 | 1 | 4 |  |  |

## Problem J. Joining Cats

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
256 mebibytes

Suzukaze Aoba has a magical fan. There are $n$ cats sitting on a straight line. Aoba wonders if she can merge all cats into one by using the magical fan $k$ times.
The $i$-th activation of the fan produces a gust of wind of strength exactly $s_{i}$.
For each gust of wind, Aoba picks its starting position and direction (eastward or westward). Then the gust of wind starts moving continuously in that direction with constant speed. Aoba can decide to turn the fan off at any moment, in which case, the wind disappears.
When the gust of wind encounters a cat, if the weight of the cat is strictly larger than the strength of the wind, the fan turns off automatically. Otherwise, the cat will be continuously pushed to the direction the wind is blowing.
When two cats meet, they merge into a cat whose weight is equal to the sum of their weights. The above rules then apply to the newly merged cat.
Determine if joining all cats is possible by using the fan at most $k$ times.

## Input

The first line contains two integers $n$ and $k(1 \leq n, k \leq 5000)$.
The second line contains $n$ integers $w_{1}, \ldots, w_{n}\left(1 \leq w_{i} \leq 10^{9}\right)$, denoting the initial weights of the cats from left to right. No two cats initially sit on the same spot.
The third line contains $k$ integers $s_{1}, \ldots, s_{k}\left(1 \leq s_{i} \leq 10^{9}\right)$.

## Output

Print a line with one word (case-sensitive): "Yes" if it is possible to merge all cats into one by using the magical fan at most $k$ times, or "No" otherwise.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{llll} \hline 5 & 2 & & \\ 1 & 1 & 1 & 1 \\ 2 & 2 & & \\ \hline \end{array}$ | Yes |
| $\begin{array}{llllllll} \hline 6 & 7 & & & & \\ 3 & 2 & 1 & 1 & 2 & 3 & \\ 2 & 2 & 2 & 2 & 2 & 2 & 2 \end{array}$ | No |
| $\begin{array}{lllllll} \hline 7 & 4 & & & & & \\ 1 & 2 & 3 & 4 & 3 & 2 & 1 \\ 3 & 3 & 3 & 3 & & & \end{array}$ | Yes |
| $\begin{array}{lllll} 5 & 1 & & & \\ 5 & 4 & 3 & 2 & 1 \\ 10 & & & & \end{array}$ | Yes |

## Problem K. Keychain

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
10 seconds
256 mebibytes

Consider a two-dimensional plane and $n$ points $p_{1}, \ldots, p_{n}$ on it. Consider $n$ circles $C_{1}, C_{2}, \ldots, C_{n}$ : the $i$-th circle is centered at $p_{i}$. All the radii of the $n$ circles are $R$.
Determine the minimum value of $R$ such that one can draw another generalized circle $\Gamma$ that intersects all the $n$ circles. Please find one such $\Gamma$ as well.

- A circle $C$ with radius $r$ contains all points such that the Euclidean distance between the point and the center of the circle is exactly $r$.
- A generalized circle is either a circle or a straight line.
- We say two objects $A$ and $B$ intersect if they share a common point.


## Input

The first line contains an integer $n(1 \leq n \leq 3000)$. On each of the next $n$ lines, there will be two integers $x_{i}$ and $y_{i}$ indicating the coordinates of point $p_{i}\left(0 \leq x_{i}, y_{i} \leq 10^{5}\right)$. It is guaranteed that no two given points coincide.

## Output

On the first line, print the optimal answer $R_{\text {opt }}$.
Your output should satisfy $0 \leq R_{\text {opt }} \leq 10^{5}$.
It can be proved that the minimum value exists and is in this range.
Suppose that $\Gamma_{\text {opt }}$ intersects all $C_{1}, \ldots, C_{n}$ when $R=R_{\text {opt }}$.
It can be shown that, under the constraints in this problem, $\Gamma_{o p t}$ can be chosen to be either a circle centered at a rational coordinate, or a straight line with integer coefficients.

- In the circle case, print "C $X Y Z r$ ", which means that the radius is $r$, and the center of the circle is $O=(X / Z, Y / Z)$.
The values $X, Y, Z$ must be integers with absolute value not greater than $10^{18}$. The value $r$ should be a non-negative real number not greater than $10^{18}$.
- In the straight line case, print "L $a b c$ ", which means that the line $L$ satisfies the equation $a x+b y=c$.
The values $a, b, c$ must be integers with absolute value not greater than $10^{18}$.
When checking your answer, the jury will first check whether $\Gamma_{\text {opt }}$ intersects each of the $C$ 's. This will be judged by checking:
- if $|R-r|-\varepsilon \leq d\left(O, p_{i}\right) \leq R+r+\varepsilon$ in the circle case $\left(d\left(O, p_{i}\right)\right.$ is the Euclidean distance between $p_{i}$ and $O$ ),
- or $R \leq d\left(L, p_{i}\right)+\varepsilon$ in the line case $\left(d\left(L, p_{i}\right)\right.$ is the distance from point $p_{i}$ to line $\left.L\right)$.

Here, $\varepsilon=10^{-6}$.
After that, your answer will be considered correct if the absolute or relative error between your $R_{\text {opt }}$ and jury's $R_{\text {opt }}$ doesn't exceed $10^{-6}$.

The 2nd Universal Cup

## Examples

|  | standard input |  |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 4 |  |  |  |  |  |  |  |
| 2 | 1 |  |  |  |  |  |  |
| 1 | 3 |  |  |  |  |  |  |
| 2 | 4 |  |  |  |  |  |  |
| 7 | 2 |  |  |  |  |  |  |
| standard output |  |  |  |  |  |  |  |
| 0.27069063257455492223 |  |  |  |  |  |  |  |
| C 11527202882.77069063257455492234 |  |  |  |  |  |  |  |



| standard input |  |  |
| :--- | :--- | :---: |
| 10 |  |  |
| 756 | 624 |  |
| 252 | 208 |  |
| 504 | 416 |  |
| 378 | 312 |  |
| 203 | 287 |  |
| 329 | 391 |  |
| 0 |  |  |
| 707 | 703 |  |
| 126 | 104 |  |
| 581 | 599 |  |
|  |  |  |
| 46.05915288207108030175 |  |  |
| L -1248 1512 90300 |  |  |

## Note

The first two examples:



Be careful of overflow. Consider using long double or __int128.

## Problem L. Lines

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 1 second |
| Memory limit: | 256 mebibytes |

Given are three arrays of $n+1$ integers: $a, b, c$.
We define $3 n+1$ functions $F_{0}, F_{1}, \ldots, F_{3 n}$ as follows:

$$
F_{i}(t)=i t+\max _{\substack{0 \leq x, y, z \leq n \\ x+y+z=i}}\left(a_{x}+b_{y}+c_{z}\right) .
$$

A function $F_{i}$ is said to be NeVeR_LosEs if and only if there does not exist a real number $t$ such that $F_{i}(t)>F_{j}(t)$ for all $j \neq i$.

Your task is to find out which functions can be called NeVeR_LosEs.

## Input

The first line contains an integer $n\left(1 \leq n \leq 3 \cdot 10^{5}\right)$.
The second line contains the array $a_{0}, a_{1}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$.
The third line contains the array $b_{0}, b_{1}, \ldots, b_{n}\left(0 \leq b_{i} \leq 10^{9}\right)$.
The fourth line contains the array $c_{0}, c_{1}, \ldots, c_{n}\left(0 \leq c_{i} \leq 10^{9}\right)$.

## Output

On the first line, print an integer $m$, the number of functions that can be called NeVeR_LosEs.
On the second line, print $m$ integers $0 \leq i_{1} \leq \ldots \leq i_{m} \leq 3 n$, the indices of these functions in ascending order.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{\|llll} \hline 3 & & & \\ 3 & 1 & 8 & 7 \\ 9 & 1 & 3 & 1 \\ 5 & 1 & 1 & 6 \end{array}$ | $\begin{array}{lllll} 5 & & & & \\ 1 & 3 & 4 & 7 & 8 \end{array}$ |
| $\begin{array}{ll} \hline 1 & \\ 1 & 2 \\ 1 & 2 \\ 1 & 2 \end{array}$ | $\begin{array}{ll} 2 \\ 12 \end{array}$ |

